

An alternative method to solve a system of one-variable linear congruences with prime moduli

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We consider a system of linear congruences of a single variable with specific conditions and construct a new faster method to solve that system without using the Chinese remainder theorem. The concerned system of congruences is $a_i x \equiv b_i \pmod{m_i}$, for $0 < a_i, b_i < m_i$ for all $i = 1, 2, 3, \dots, n$ with all m_i values are prime. This system can be reduced to a single linear congruence of the same variable and it has a unique solution. The single congruence is

$(a_1 M_1 + a_2 M_2 + \dots + a_n M_n)x \equiv (b_1 M_1 + b_2 M_2 + \dots + b_n M_n) \pmod{M}$ where $M = m_1 \times m_2 \times \dots \times m_n$ and $M_i = \frac{M}{m_i}$ for all $i = 1, 2, 3, \dots, n$.

The unique solution of the single congruence is the solution of the above system.

Keywords: Chinese remainder theorem, linear congruence and prime modulo

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