



# UNIVERSITY OF RUHUNA

## Faculty of Engineering

End-Semester 6 Examination in Engineering: February 2020

Module Number: EE6301

Module Name: Communication Systems

[Three Hours]

[Answer all questions, each question carries 10 marks]

All notations have their usual meaning.

- Q1 a) Obtain an expression for the voltage reflection coefficient at any point on a lossless transmission line, distance  $l$  away from the load end.

**Hint:**

Consider the general solution for the voltage wave equation of a transmission line is given by

$$v(z) = V^+e^{-\gamma z} + V^-e^{\gamma z}$$

where  $z$  is the distance measured from the source end of the transmission line.

[2.0 Marks]

- b) A transmission line shown in Figure Q1 feeds two parallel load impedances  $Z_{R1} = (200 + j200) \Omega$  and  $Z_{R2} = (100 - j100) \Omega$  through a half wavelength section and a quarter wavelength section respectively. The characteristic impedance of the two sections is  $200 \Omega$ . Use the provided Smith Chart to determine the followings.

- Impedance at the terminals AB.
- Position and length of the short circuited shunt stub that will match the line to the load at terminals AB.

**Note:**

Give only one solution and attach the Smith Chart to the answer script.

[8.0 Marks]

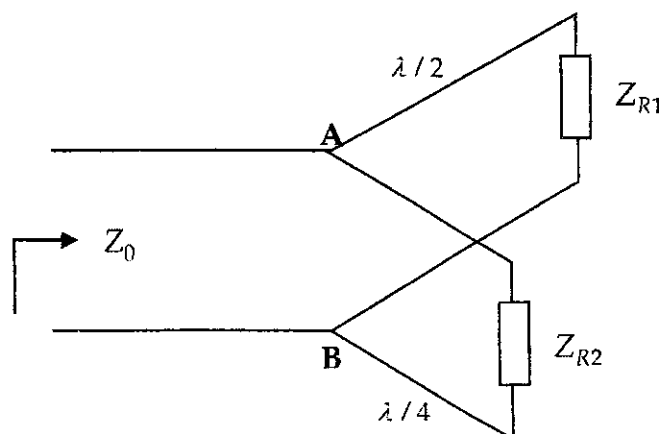


Figure Q1

- Q2 a) Explain what is meant by the dominant mode of a rectangular waveguide. [1.0 Mark]
- b) A sinusoidal wave propagating in a rectangular waveguide has the following field components in the z-direction (direction along the axis of the waveguide).

$$H_z = H_0 \cos\left(\frac{\pi z}{a}\right) e^{j(\omega t - \beta z)}$$

$$E_z = 0$$

Obtain an expression for the average power density of the waveguide.

**Hint:**

The transverse components of a rectangular waveguide are

$$E_x = \frac{1}{h^2} \left[ -\gamma \frac{\partial E_z}{\partial x} - j\omega\mu \frac{\partial H_z}{\partial y} \right], \quad E_y = \frac{1}{h^2} \left[ -\gamma \frac{\partial E_z}{\partial y} + j\omega\mu \frac{\partial H_z}{\partial x} \right],$$

$$H_x = \frac{1}{h^2} \left[ j\omega\varepsilon \frac{\partial E_z}{\partial y} - \gamma \frac{\partial H_z}{\partial x} \right] \quad \text{and} \quad H_y = \frac{1}{h^2} \left[ -j\omega\varepsilon \frac{\partial E_z}{\partial x} - \gamma \frac{\partial H_z}{\partial y} \right].$$

Moreover, the time-average Poynting vector in a rectangular waveguide is

$$P = \frac{1}{2} \text{Re}[\mathbf{E} \times \mathbf{H}].$$

[6.0 Marks]

- c) Hence, draw the electric and magnetic field patterns for the mode mentioned in part b) of the rectangular waveguide. [3.0 Marks]

- Q3 a) A two-ray ground reflection model is shown in Figure Q3. If  $E_0$  is the free space Electric field (in V/m) at a reference distance  $d_0$  from the transmitting antenna, electric field components in the direct path and the reflected path are  $E_D = \frac{E_0 d_0}{r_1}$

and  $E_R = \frac{\alpha E_0 d_0}{r_1}$  respectively, where  $\alpha = \left( \frac{G_R}{G_D} \right)^{1/2} \frac{r_1}{r_2} \rho D$ .

- i) Explain why it is used two factors  $\rho$  and  $D$  in deriving the aforementioned electric field components.
- ii) Show that the total electric field is given by  $E_T = \frac{2E_0 d_0}{d} \frac{2\pi h_t h_r}{\lambda d}$ , when  $d \gg r_1, r_2$ .

[4.0 Marks]

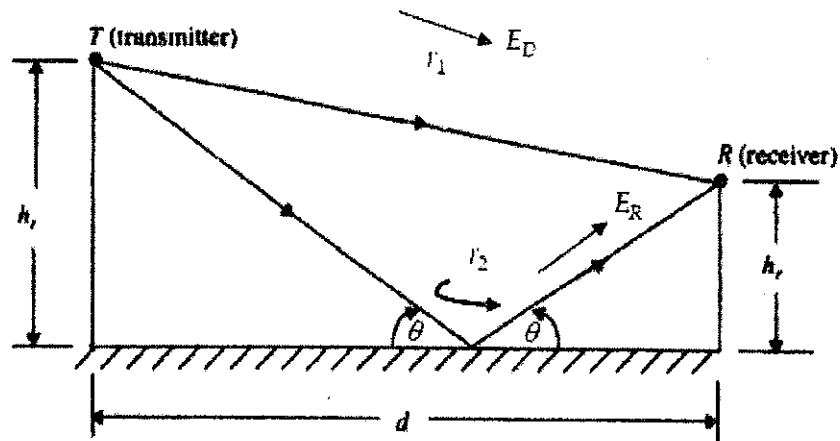


Figure Q3

- b) A mobile located 5 km away from a base station, uses a vertical  $\lambda/4$  monopole antenna with a gain of 2.55 dB to receive cellular radio signals. The electric field at 1 km away from the transmitter is measured to be  $10^{-3}$  V/m. The carrier frequency used for this system is 900 MHz.

- i) Determine the effective aperture of the receiving antenna.
- ii) Determine the received power at the mobile using the two-ray ground reflection model assuming the heights of transmitting and receiving antennas 50 m and 1.5 m respectively.

[6.0 Marks]

- Q4 a) Briefly explain the following terms related to an antenna.

- i) Directive Gain
- ii) Power Gain

[2.0 Marks]

- b) A Hertzian dipole at length  $l$  ( $l \ll \lambda$ ), placed at the origin and oriented along z-axis has following non-zero electric and magnetic field components for a spherical coordinate system.

$$E_{\theta} = \frac{I_0 l \sin \theta e^{j\omega t} e^{-j\beta r}}{4\pi\omega\epsilon} \left\{ \frac{j\beta^2}{r} + \frac{\beta}{r^2} - \frac{j}{r^3} \right\}$$

$$E_r = \frac{I_0 l \cos \theta e^{j\omega t} e^{-j\beta r}}{4\pi\omega\epsilon} \left\{ \frac{\beta}{r^2} - \frac{j}{r^3} \right\}$$

$$H_{\phi} = \frac{I_0 l \sin \theta e^{j\omega t} e^{-j\beta r}}{4\pi r} \left\{ j\beta + \frac{1}{r} \right\}$$

Suppose that  $I_0$  is the constant current along the length of the dipole.

- i) Modify the given expression by neglecting the higher order terms of parameter  $r$ , when  $r \gg \lambda$ .
- ii) Show that  $\frac{E_\theta}{H_\phi}$  gives the characteristic impedance of the free space.

[5.0 Marks]

- c) Figure Q4 shows the spatial variation of the three fields, radiation field (with  $1/r$  terms), induction field (with  $1/r^2$  terms) and electro-static field (with  $1/r^3$  terms). Using the figure, explain the difference between the near-field and the far-field of a Hertzian dipole antenna.

[3.0 Marks]

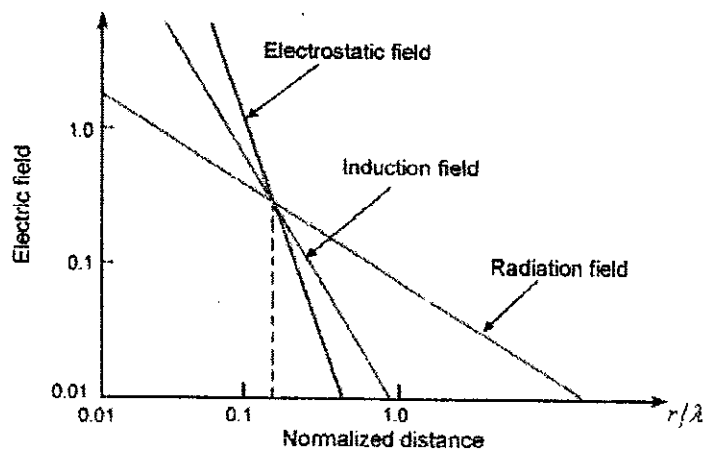


Figure Q4

- Q5 a) A block diagram of a satellite transponder is shown in Figure Q5. Briefly explain the purpose of each block to identify the basic operations of the transponder.

[3.0 Marks]

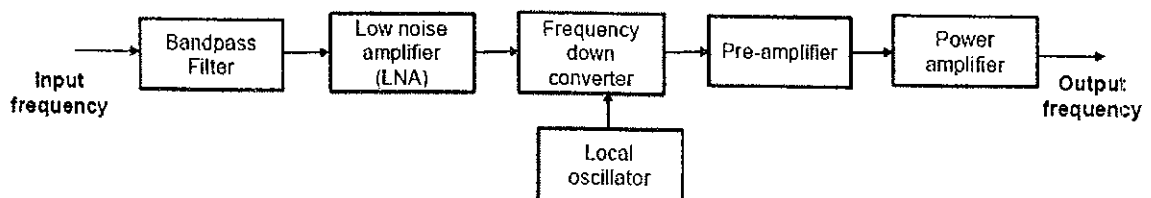


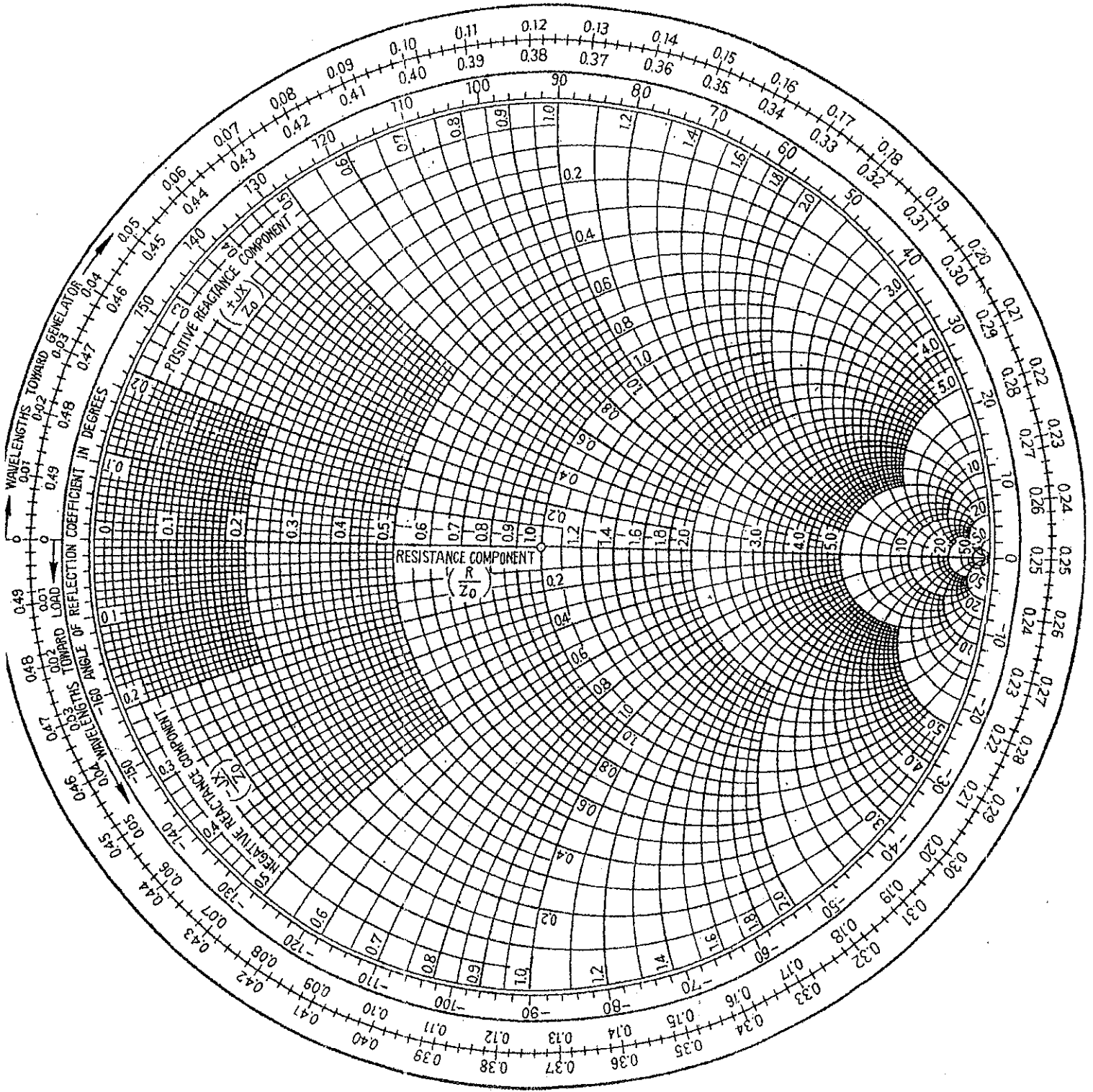
Figure Q5

- b) A 14/11 GHz digital satellite, transparent transponder and communication link has the following specifications.

Uplink Saturating Flux Density	-83.2 dBW/m <sup>2</sup>
Input Back-off Loss	8.0 dB
Satellite Gain-to-Noise Temperature Ratio	1.8 dB/K
Transponder Bandwidth	36 MHz
Uplink Slant Range	41000 km
Saturated Satellite Effective Isotropic Radiated Power (EIRP)	45 dBW
Output Back-off Loss	2.8 dB
Downlink Slant Range	39000 km
Earth Station Gain-to-Noise Temperature Ratio	31 dB/K
Downlink Earth Station Fixed Losses	3.5 dB

If the uplink and downlink earth station elevations angles are  $5.6^\circ$  and  $20.3^\circ$  respectively, estimate the overall link, clear sky, carrier-to-noise (CNR) ratio. Assume pure TDMA operation such that there is no intermodulation noise and interference is negligible. Further, the characteristic impedance of the free space is  $120\pi$ .

[7.0 Marks]



The Smith Chart