



# UNIVERSITY OF RUHUNA

Faculty of Engineering

End-Semester 8 Examination in Engineering: December 2018

Module Number: EE8208

Module Name: Intelligent Systems Design

[Three Hours]

[Answer all questions, each question carries 15 marks]

- Q1. a) Briefly explain what does it mean by supervised learning and unsupervised learning of Artificial Neural Networks. [5 Marks]
- b) Describe the following activation functions.
- i. Hard Limit Function
  - ii. Log Sigmoid Function [4 Marks]
- c) Consider two input/output data sets of a neural network.

$$\left\{ \left( \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}, 1 \right), \left( \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix}, 0 \right) \right\}$$

Let the initial weights and bias are given as  $W = [0.1 \ -0.1 \ 0.1]$  and  $b = 0.5$  respectively. Determine the weight vector and the bias if the network trained by the perceptron learning rule when the learning rate  $m = 1$ . [6 Marks]

- Q2. a) i Explain what is meant by orthonormal vectors.
- ii Show that  $x_1, x_2$  of the following input/output vectors are orthonormal.

$$(x_1, t_1) = \left( \begin{bmatrix} 0.5 \\ -0.5 \\ 0.5 \\ -0.5 \end{bmatrix}, \begin{bmatrix} 1 \\ 1 \end{bmatrix} \right) \quad (x_2, t_2) = \left( \begin{bmatrix} -0.5 \\ -0.5 \\ 0.5 \\ 0.5 \end{bmatrix}, \begin{bmatrix} -1 \\ 1 \end{bmatrix} \right)$$

Use Hebbian rule to determine the weight vector for the network of  $(x_1, t_1)$  and  $(x_2, t_2)$  [5 Marks]

- b) i Write down the 4 major steps of Back Propagation algorithm.
- ii Train the below specified neural network with the data set  $\left( \begin{bmatrix} 1 \\ -1 \end{bmatrix}, 1 \right)$  by using the backpropagation algorithm, and compute the output error after first 2 iterations.

Hidden layer of the Neural Network contains 3 neurons and the initial weights between the input layer and the hidden layer are

$$W = \begin{bmatrix} 0.1 & 0.2 \\ -0.1 & 0.1 \\ 0.2 & -0.1 \end{bmatrix}$$

and weights between hidden layer and output layer are

$$V = [0.1 \ -0.1 \ 0.2].$$

Use log sigmoid and linear activation functions for hidden and output layers respectively, and learning rate is 0.1.

Hint: The delta value of output and hidden layers ( $h$ ) are given in usual notations by

$$\delta_j = e_j f'_o(\text{net}_j)$$

$$\text{and } \delta_j^h(n) = f'_h(\text{net}_j^h(n)) \sum_{k=1}^{h+1} \delta_k^{h+1}(n) w_{kj}^{h+1}(n)$$

Weight between  $j^{\text{th}}$  neurons of  $h^{\text{th}}$  hidden layer  $k^{\text{th}}$  neurons ( $h + 1$ ) hidden layer is updated in  $n^{\text{th}}$  iteration according to the equation

$$w_{ji}(n + 1) = w_{ji}(n) + \eta_j \delta_j f'_h(\text{net}_i)$$

[10 Marks]

- Q3. a) Describe what are *linguistic variable* and the *values* it can take. Use an appropriate example to answer. [3 Marks]
- b) Compare and contrast *classical Set* and *Fuzzy Set*. [3 Marks]
- c) Define fuzzy sets Cold, Cool, Pleasant, Warm and Hot to represent room temperature, appropriately for local conditions. Clearly define the Universe of Discourse. [3 Marks]
- d) Define operations i)  $\min(\mu_A, \mu_B)$ , ii)  $\max(\mu_A, \mu_B)$ , iii)  $1 - \mu_A$ , iv)  $\min[\mu_A + \mu_B, 1]$ , by using the Membership Functions of the Fuzzy Sets A and B. Also interpret these operations in diagrams of Universe of Discourse vs Fuzzy Membership and mention alternative names used for these operations [3 Marks]
- e) Explain how to evaluate a rule of type "If x is A AND y is B THEN z is C" by using an appropriate membership functions and operators. [3 Marks]

Q4. A Fuzzy Logic controller is to be designed for a classical feedback control system.

- a) Draw the classical feedback control diagram with Process, Fuzzy Controller and the feedback path. Define the Control Error  $e(k)$  and Rate of Error  $r(k)$  with respect to the SV (Set Value) and PV (Process Value). [2.0 Marks]
- b) Define an appropriate Rule Base for control action, based on the Linguistic Variables; Error  $e(k)$ , Rate of Error  $r(k)$  and Control Output  $du(k)$ , with meaningful linguistic values. [2.0 Marks]
- c) Define the membership functions for the linguistic values identified in b) and show them in diagrams; Membership vs Universe of Discourse. [3.0 Marks]
- d) Show how to calculate the Control Output  $du(k)$  for a given values of  $e(k)$  and  $r(k)$  by using a numerical example. Use the method "Center of Gravity" to calculate the  $du(k)$ . [3.0 Marks]
- e) Re-design the Rule Base if the controller inputs are Error  $e(k)$ , Rate of Error  $r(k)$  and Sum of Error  $\sum e(k)$  for  $k=k, k-1, ..k-50$ . [5 Marks]