



**NOTES:**

Use carefully labelled sketches to support your answers where necessary.  
You may make additional assumptions, but clearly state them in your answers.  
Data and formulae are given in page 4.

- Q1. a) On a schematic diagram, show all the key control surfaces of an aircraft. Also briefly describe the function of each of them. [2.0 Marks]
- b) Define the terms "absolute height" and "geopotential height". [2.0 Marks]
- c) Comment on the statement: "Boundary layer development over the fuselage does not affect the accurate static pressure measurements in an aircraft." [2.0 Marks]
- d) During a cruising phase of an aircraft, it was recorded that the air speed indicator reading (ASIR) as 187 knots. As a result of errors in pressure measurements, it was found that static pressure error was -210 Pa. If the instrument error correction for the air speed indicator (ASI) is +0.8 knots, estimate the pressure error correction for the ASI, assuming that the pitot pressure error is zero. [6.0 Marks]
- Q2. a) Describe stalling patterns for a rectangular wing, a tapered wing, and an elliptic wing. [2.0 Marks]
- b) What is your recommendations for optimum taper ratio and position of the control surfaces in relation to a tapered wing? Justify your answer. [3.0 Marks]
- c) Explain the statement: "Increasing in the aspect ratio is not a viable solution to minimize the drag acted on passenger transport aircraft." [3.0 Marks]
- d) An elliptic lift distribution pattern is given with usual notations by;

$$L(y) = \rho_{\infty} V_{\infty} \Gamma_0 \sqrt{1 - \left(\frac{2y}{b}\right)^2}$$

Hence show that, for a wing having elliptic planform shape has a constant local lift coefficient throughout its span.

[4.0 Marks]

Q3. a) Draw the variation of lift coefficient with respect to angle of attack for the following airfoil shapes.

- i. NACA 0016
- ii. NACA 5400

[2.0 Marks]

b) Explain the statement, "Even though airfoil is a streamline body, the flow trends to separate towards the trailing edge (TE) of the airfoil".

[3.0 Marks]

c) Consider an airfoil with chord length  $c$  and the running distance  $x$  measured along the chord. The leading edge is located at  $x/c = 0$  and the trailing edge at  $x/c = 1$ . The pressure coefficient variations over upper and lower surfaces are given by following three expressions:

$$C_{p1} = 1 - 300 \left( \frac{x}{c} \right)^2 \text{ for } 0 \leq x/c \leq 0.1,$$

$$C_{p2} = -2.2277 + 2.2277 \left( \frac{x}{c} \right)^2 \text{ for } 0.1 < x/c \leq 1,$$

$$C_{p3} = 1 - 0.95 \left( \frac{x}{c} \right) \text{ for } 0 \leq x/c \leq 1.$$

- i. What are the expressions from above that show  $C_p$  variations over the upper surface of the airfoil? Justify your answer.
- ii. Estimate the lift coefficient of the airfoil.

[7.0 Marks]

Q4. a) Write the most general expression for total drag acted on a finite wing. Also state the main sources of the drag for each term in your expression.

[2.0 Marks]

b) Describe how the wave drag is generated on airfoils.

[2.0 Marks]

c) The wings of an Unmanned Aerial Vehicle (UAV) are made of NACA 23015 airfoil section. The tapered planform wings have a total span of 38 m; while the root chord length and the tip chord length are 6.5 m and 1.7 m, respectively. The UAV cruises with 28 km/h at an altitude of 20 km, where the density and the kinematic viscosity of air are  $0.158 \text{ kgm}^{-3}$  and  $16.312 \times 10^{-6} \text{ m}^2/\text{s}$ , respectively.

The lift coefficient and the drag coefficient variations for the NACA 23015 as a function of AoA are presented in Table Q4 and the efficiency factor for the wing is 0.95. Taking  $\tau = 0.55$ , and if the UAV is at  $5^\circ$  of angle of attack, determine;

- i. Reynolds number of the UAV,
- ii. Lift and drag coefficient,
- iii. The gross mass of the UAV.

[8.0 Marks]

- Q5. a) Write key steps in negative rolling of an aircraft. What is the sign of control surface deflection? Justify your answer. [2.0 Marks]
- b) Define the aerodynamic center of an airfoil. Show that for an airfoil, the aerodynamic center is located at 25% of the chord length. [2.0 Marks]
- c) What is the requirement for a statically stable aircraft? Explain your answer. [2.0 Marks]
- d) On a schematic diagram, mark all the forces acted on an aircraft in a pure longitudinal flight and Then derive all the modelling equations. You may take all the relevant angles to be small. Hence,
- i. Derive symbolic expressions for the equilibrium angle of attack ( $\alpha_e$ ),
  - ii. Obtain expressions for changes in equilibrium angle of attack ( $\Delta\alpha_e$ ) when the pilot has increased the elevator command by an amount of  $\delta m$ .
- [6.0 Marks]

Table Q4: NACA 23015 airfoil data

Angle of Attack (AoA) (in degrees)	Lift coefficient - $c_l$	Drag coefficient - $c_d$
-4	-0.24	0.008
-2	0.08	0.006
0	0.4	0.006
2	0.72	0.006
4	1.04	0.007
6	1.36	0.0075
8	1.68	0.0092
10	2.00	0.0098

## Data & formulae sheet

a.) True air speed of an aircraft is given by:

$$V = \sqrt{\frac{2\gamma P_\infty}{\gamma - 1 \rho_\infty} \left[ \left[ 1 + \frac{P_T - P_\infty}{P_\infty} \right]^\frac{\gamma-1}{\gamma} - 1 \right]}$$

b.) Airfoil lift curve slope  $a_0$  and 3-D wing lift curve slope  $a_1$  are related as:

$$a_1 = \frac{a_0}{1 + \left( \frac{a_0}{\pi AR} \right) (1 + \tau)}$$

c.) For an airfoil, the lift coefficient is given by:

$$c_l = \left[ \int_0^1 (C_{p,l} - C_{p,u}) d\left(\frac{x}{c}\right) \right]$$

d.) 1 knot = 0.5144 ms<sup>-1</sup>.