University of Ruhuna

2017/2018 Academic Year Master of Arts in Economics

1st Semester End Examination - Dec. 2018/ January 2019

MAE 5102 –Economic Statistics

Answer any **Four (04)** questions.

Time: 3 Hours

1.

a. There are two distinct divisions of statistics that is a "descriptive statistics" and "inferential statistics". The role of the descriptive statistics is to transform data into information. You are required to confirm whether the statements is true or false with evidence.

(03 Marks)

b. Give four sources of secondary data in Sri Lankan context.

(02 Marks)

c. A particular food item is sold at market was examined and drawn a random sample of 10 items. The weight of the items observed for nearest gram and resulted values are summarized below.

66, 71, 71, 60, 68, 66, 68, 71, 66, 67

Illustrates this information with ungrouped frequency distribution.

(04 Marks)

d. Explain the following terms/concepts with suitable examples

(i). Grouped frequency distribution

(ii). Class intervals

(iii). Class boundaries

(06 Marks)

2.

a. Give sufficient evidence to state whether the following statements are true or false.

(i). The median is less than the mode for positively skewed frequency distributions.

(ii). As a measure of central tendency, mean is free from the effect of extreme values.

(04 Marks)

b. Following table provides information regarding the age of 100 employees of a particular organization. Compute the mean age of an employee in this firm.

Age group	Number of employees
60 – 62	05
63 – 65	18
66 – 68	42
69 – 71	27
72 – 74	08

(04 Marks)

c. A kind of biscuit is packed by two machines – A and B. A researcher has drawn a random sample of size 10 0f such biscuit packets and measured the weight to the nearest gram. Following table provides these information and you are required to compute the standard deviations of packing process of machines and comments.

Machine A (grams)	196, 198, 198, 199, 200, 200, 201, 201, 202, 205
Machine B (grams)	192, 194, 195, 198, 200, 201, 203, 204, 206, 207

(07 Marks)

(08

3.

a. A committee consisting of 5 members votes on whether or not to hire a new candidate for a certain post. There are two candidates and the probability that each member's vote for first candidate is 0.6 which does not change. Only if half of the committee agrees to hire candidate will receive the offer. Each member should vote for one of the two candidates since they cannot avoid from voting.

(i). What is the probability that the first candidate gets the offer?

(ii). What is the probability that exactly three members vote for the first candidate?

(iii). What is the probability that none of the members do not vote for the second candidate?

(9 Marks)

b. X is a discrete random variable and it has Poisson distribution with the expected value of 05.

(i). Find P(X=4)

(ii). Find F(3) for X

(iii). Find E(2X)

(06 Marks)

4.

a. X is a continuous random variable which has a normal distribution. Mean of X is 350 and standard deviation is 110.

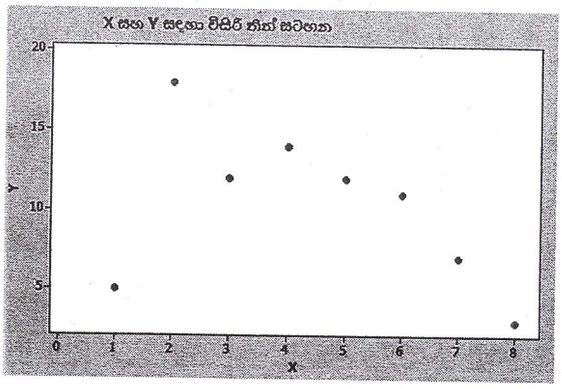
(i). Find the probability that X less than 400.

(ii). Find the probability that X lies between 250 and 400.

(06 Marks)

b.

(i). Explain the correlation between X and Y according to the following scatter plot.



(ii). The simple linear regression equation which was derived by the method of ordinary least square for above X and Y is as follows.

$$Y = 14.2 - 0.881X$$

Interpret the regression coefficients.

(iii). Do the conclusions drawn by correlation and regression are consistent?

(iv). The coefficient of determination for the above linear regression model is equal to 0.23. What can you say about the reliability of a regression model?

(v). Estimate the value of Y when X=12

(09 Marks)

5. Answer all parts of the following questions

a. Glass manufactured by a company is tested for thickness. The test gives a correct positive result with a probability of 0.90 when the thickness of glass is the acceptable level, but gives an incorrect positive result (false positive) with a probability of 0.05 when in fact the thickness of glass is not the acceptable level. If 97% of the glass' thickness are the acceptable level, and a glass chosen at random fails the test, what is the probability it really thickness is not the acceptable level?

(07 Marks)

b. There are 16 members in cricket pool with 9 members are batsmen and remains are bowlers. 11 members team should be formed from this pool.

(i). How many team can be formed with 6 batsmen and 5 bowlers?

(02 Marks)

(ii). If pre-selected batman and bowler from the pool must be two members of the team, how many team can be formed with at least 5 batsmen and 4 bowlers?

(04 marks)

c. Kawya is going to choose the size, color, phrase, and picture for a New Year card for her friend. There are 3 sizes, 5 colors, 6 phrases, and 3 pictures for her to choose from. (The printing company charges a fee to add extra design elements, so she will choose only one of each.) How many different card designs are possible?

(02 Marks)

6. Answer all parts of the following questions:

a. Accordingly the records of a bank who issued credit card, average monthly usage of their credit cards is 15000 Rupees. The bank launched the promotion campaign and after one month of the campaign the bank collected monthly usage of their credit cards of 61 card holders who selected randomly. Mean monthly usage of the credit card of the sample was 18000 Rupees with a standard deviation of 5000 Rupees. The bank data analyst need to test the sample whether the promotion campaign was effective using 0.1 significant level.

Answer for following questions assuming that the bank data analyst test the data using statistical analysis.

(i). Define Null and Alternative Hypotheses (01 Marks)

(ii). State Alpha (01 Marks)

(iii). State Decision Rule (01 Marks)

(iv). Calculate Test Statistic (02 Marks)

(v). State Results (01 Marks)

(vi). State the decision which can be made by the data analyst. (02 Marks)

b. Agricultural service center of one of the area distributed seed of the vegetables to the farmers of the area. However, particular farmer was allowed take only one type of seed of the vegetable. Following table shows details of 100 farmers with their collected seeds of vegetable types.

Seed of Vegetable type	Number of farmers
A	16
B	24
C	23
D	18
E	19

Analyze to check whether number of farmers who took each vegetable type in free of cost are in equal proportion under 5% significant level.

(i). Define Null and Alternative Hypotheses

(01 Marks)

(ii). Calculate Test Statistic

(03 Marks)

(iii). State the decision.

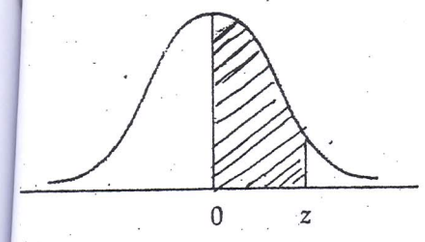
(03 Marks)

@@@@@@@@@@@

Following Equations can be used if required:

1. $P(A\ or\ B) = P(A) + P(B) - P(A\ and\ B)$.
2. $P(A\ and\ B) = P(A \backslash B)\ P(B)$
3. $P(B_i|\ A) = \frac{P(A\,|B_i)P(B_i)}{\sum_{i=1}^{n} P(A\,|\,B_i)P(B_i)}$
4. $\bar{x} \pm Z\frac{s}{\sqrt{n}}$
5. $\hat{p} \pm z^*\left(\sqrt{\frac{\hat{p}(1-\hat{p})}{n}}\right)$
6. $s = \sqrt{\frac{1}{n-1}\sum_i^n (x_i - \bar{x})^2}$
7. $Z^* = \frac{\hat{p}-p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$
8. $t^* = \frac{\bar{x}-\mu_0}{S/\sqrt{n}}$
9. $\chi^2 = \sum\left[\frac{(O_i - E_i)^2}{E_i}\right]$

mal Curve Areas



	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990

SOURCE: Abridged from Table 1 of A. Hald, *Statistical Tables and Formulas* (New York: Wiley & Sons, Inc.), 1952. Reproduced by permission of A. Hald and the publisher, John Wiley & Sons, Inc.

t Table

cum. prob	$t_{.50}$	$t_{.75}$	$t_{.80}$	$t_{.85}$	$t_{.90}$	$t_{.95}$	$t_{.975}$	$t_{.99}$	$t_{.995}$	$t_{.999}$	$t_{.9995}$
one-tail	**0.50**	**0.25**	**0.20**	**0.15**	**0.10**	**0.05**	**0.025**	**0.01**	**0.005**	**0.001**	**0.0005**
two-tails	**1.00**	**0.50**	**0.40**	**0.30**	**0.20**	**0.10**	**0.05**	**0.02**	**0.01**	**0.002**	**0.001**
df											
1	0.000	1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.31	636.62
2	0.000	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	22.327	31.599
3	0.000	0.765	0.978	1.250	1.638	2.353	3.182	4.541	5.841	10.215	12.924
4	0.000	0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	0.000	0.727	0.920	1.156	1.476	2.015	2.571	3.365	4.032	5.893	6.869
6	0.000	0.718	0.906	1.134	1.440	1.943	2.447	3.143	3.707	5.208	5.959
7	0.000	0.711	0.896	1.119	1.415	1.895	2.365	2.998	3.499	4.785	5.408
8	0.000	0.706	0.889	1.108	1.397	1.860	2.306	2.896	3.355	4.501	5.041
9	0.000	0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.297	4.781
10	0.000	0.700	0.879	1.093	1.372	1.812	2.228	2.764	3.169	4.144	4.587
11	0.000	0.697	0.876	1.088	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	0.000	0.695	0.873	1.083	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	0.000	0.694	0.870	1.079	1.350	1.771	2.160	2.650	3.012	3.852	4.221
14	0.000	0.692	0.868	1.076	1.345	1.761	2.145	2.624	2.977	3.787	4.140
15	0.000	0.691	0.866	1.074	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16	0.000	0.690	0.865	1.071	1.337	1.746	2.120	2.583	2.921	3.686	4.015
17	0.000	0.689	0.863	1.069	1.333	1.740	2.110	2.567	2.898	3.646	3.965
18	0.000	0.688	0.862	1.067	1.330	1.734	2.101	2.552	2.878	3.610	3.922
19	0.000	0.688	0.861	1.066	1.328	1.729	2.093	2.539	2.861	3.579	3.883
20	0.000	0.687	0.860	1.064	1.325	1.725	2.086	2.528	2.845	3.552	3.850
21	0.000	0.686	0.859	1.063	1.323	1.721	2.080	2.518	2.831	3.527	3.819
22	0.000	0.686	0.858	1.061	1.321	1.717	2.074	2.508	2.819	3.505	3.792
23	0.000	0.685	0.858	1.060	1.319	1.714	2.069	2.500	2.807	3.485	3.768
24	0.000	0.685	0.857	1.059	1.318	1.711	2.064	2.492	2.797	3.467	3.745
25	0.000	0.684	0.856	1.058	1.316	1.708	2.060	2.485	2.787	3.450	3.725
26	0.000	0.684	0.856	1.058	1.315	1.706	2.056	2.479	2.779	3.435	3.707
27	0.000	0.684	0.855	1.057	1.314	1.703	2.052	2.473	2.771	3.421	3.690
28	0.000	0.683	0.855	1.056	1.313	1.701	2.048	2.467	2.763	3.408	3.674
29	0.000	0.683	0.854	1.055	1.311	1.699	2.045	2.462	2.756	3.396	3.659
30	0.000	0.683	0.854	1.055	1.310	1.697	2.042	2.457	2.750	3.385	3.646
40	0.000	0.681	0.851	1.050	1.303	1.684	2.021	2.423	2.704	3.307	3.551
60	0.000	0.679	0.848	1.045	1.296	1.671	2.000	2.390	2.660	3.232	3.460
80	0.000	0.678	0.846	1.043	1.292	1.664	1.990	2.374	2.639	3.195	3.416
100	0.000	0.677	0.845	1.042	1.290	1.660	1.984	2.364	2.626	3.174	3.390
1000	0.000	0.675	0.842	1.037	1.282	1.646	1.962	2.330	2.581	3.098	3.300
Z	0.000	0.674	0.842	1.036	1.282	1.645	1.960	2.326	2.576	3.090	3.291
	0%	50%	60%	70%	80%	90%	95%	98%	99%	99.8%	99.9%
	Confidence Level										

mulative probability distribution of Poisson Distribution

λ =	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
X=0	0.6065	0.3679	0.2231	0.1353	0.0821	0.0498	0.0302	0.0183	0.0111	0.0067
1	0.9098	0.7358	0.5578	0.4060	0.2873	0.1991	0.1359	0.0916	0.0611	0.0404
2	0.9856	0.9197	0.9197	0.8088	0.6767	0.5438	0.4232	0.3208	0.2381	0.1247
3	0.9982	0.9810	0.9344	0.8571	0.7576	0.6472	0.5366	0.4335	0.3423	0.2650
4	0.9998	0.9963	0.9814	0.9473	0.8912	0.8153	0.7254	0.6288	0.5321	0.4405
5	1.0000	0.9994	0.9994	0.9955	0.9834	0.9161	0.8576	0.7851	0.7029	0.6160
6	1.0000	0.9999	0.9991	0.9955	0.9858	0.9665	0.9347	0.8893	0.8311	0.7622
7	1.0000	1.0000	0.9998	0.9989	0.9958	0.9881	0.9733	0.9489	0.9134	0.8666
8	1.0000	1.0000	1.0000	0.9998	0.9989	0.9962	0.9901	0.9786	0.9597	0.9319
9	1.0000	1.0000	1.0000	1.0000	0.9997	0.9989	0.9967	0.9919	0.9829	0.9682
10	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9990	0.9972	0.9933	0.9863

BINOMIAL DISTRIBUTION

$$P(X \le x) = \sum_{r=0}^{x} {}^{n}C_{r} p^{r} (1-p)^{n-r}$$

1	0	0.9000	0.8500	0.8000	0.7500	0.7000	0.6500	0.6000	0.5500	0.5000
	1	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
2	0	0.8100	0.7225	0.6400	0.5625	0.4900	0.4225	0.3600	0.3025	0.2500
	1	0.9900	0.9775	0.9600	0.9375	0.9100	0.8775	0.8400	0.7975	0.7500
	2	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
3	0	0.7290	0.6141	0.5120	0.4219	0.3430	0.2746	0.2160	0.1664	0.1250
	1	0.9720	0.9393	0.8960	0.8438	0.7840	0.7183	0.6480	0.5748	0.5000
	2	0.9990	0.9966	0.9920	0.9844	0.9730	0.9571	0.9360	0.9089	0.8750
	3	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
4	0	0.6561	0.5220	0.4096	0.3164	0.2401	0.1785	0.1296	0.0915	0.0625
	1	0.9477	0.8905	0.8192	0.7383	0.6517	0.5630	0.4752	0.3910	0.3125
	2	0.9963	0.9880	0.9728	0.9492	0.9163	0.8735	0.8208	0.7585	0.6875
	3	0.9999	0.9995	0.9984	0.9961	0.9919	0.9850	0.9744	0.9590	0.9375
	4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
5	0	0.5905	0.4437	0.3277	0.2373	0.1681	0.1160	0.0778	0.0503	0.0313
	1	0.9185	0.8352	0.7373	0.6328	0.5282	0.4284	0.3370	0.2562	0.1875
	2	0.9914	0.9734	0.9421	0.8965	0.8369	0.7648	0.6826	0.5931	0.5000
	3	0.9995	0.9978	0.9933	0.9844	0.9692	0.9460	0.9130	0.8688	0.8125
	4	1.0000	0.9999	0.9997	0.9990	0.9976	0.9947	0.9898	0.9815	0.9688
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
6	0	0.5314	0.3771	0.2621	0.1780	0.1176	0.0754	0.0467	0.0277	0.0156
	1	0.8857	0.7765	0.6554	0.5339	0.4202	0.3191	0.2333	0.1636	0.1094
	2	0.9842	0.9527	0.9011	0.8306	0.7443	0.6471	0.5443	0.4415	0.3438
	3	0.9987	0.9941	0.9830	0.9624	0.9295	0.8826	0.8208	0.7447	0.6563
	4	0.9999	0.9996	0.9984	0.9954	0.9891	0.9777	0.9590	0.9308	0.8906
	5	1.0000	1.0000	0.9999	0.9998	0.9993	0.9982	0.9959	0.9917	0.9844
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
7	0	0.4783	0.3206	0.2097	0.1335	0.0824	0.0490	0.0280	0.0152	0.0078
	1	0.8503	0.7166	0.5767	0.4449	0.3294	0.2338	0.1586	0.1024	0.0625
	2	0.9743	0.9262	0.8520	0.7564	0.6471	0.5323	0.4199	0.3164	0.2266
	3	0.9973	0.9879	0.9667	0.9294	0.8740	0.8002	0.7102	0.6083	0.5000
	4	0.9998	0.9988	0.9953	0.9871	0.9712	0.9444	0.9037	0.8471	0.7734
	5	1.0000	0.9999	0.9996	0.9987	0.9962	0.9910	0.9812	0.9643	0.9375
	6	1.0000	1.0000	1.0000	0.9999	0.9998	0.9994	0.9984	0.9963	0.9922
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

continue;

Table A-3 The Chi-Square Table

Numbers in the table represent Chi-square values whose area to the right equals *p*.

df / p	0.10	0.05	0.025	0.01	0.005
1	2.71	3.84	5.02	6.64	7.88
2	4.61	5.99	7.38	9.21	10.60
3	6.25	7.82	9.35	11.35	12.84
4	7.78	9.49	11.14	13.28	14.86
5	9.24	11.07	12.83	15.09	16.75
6	10.65	12.59	14.45	16.81	18.55
7	12.02	14.07	16.01	18.48	20.28
8	13.36	15.51	17.54	20.09	21.96
9	14.68	16.92	19.02	21.67	23.59
10	15.99	18.31	20.48	23.21	25.19
11	17.28	19.68	21.92	24.73	26.76
12	18.55	21.03	23.34	26.22	28.30
13	19.81	22.36	24.74	27.69	29.819
14	21.06	23.69	26.12	29.14	31.32
15	22.31	25.00	27.49	30.58	32.80
16	23.54	26.30	28.85	32.00	34.27
17	24.77	27.59	30.19	33.41	35.72
18	25.99	28.87	31.53	34.81	37.16
19	27.20	30.14	32.85	36.19	38.58
20	28.41	31.41	34.17	37.57	40.00
21	29.62	32.67	35.48	38.93	41.40
22	30.81	33.92	36.78	40.29	42.80
23	32.01	35.17	38.08	41.64	44.18
24	33.20	36.42	39.36	42.98	45.56
25	34.38	37.65	40.65	44.31	46.93
26	35.56	38.89	41.92	45.64	48.29
27	36.74	40.11	43.20	46.96	49.65
28	37.92	41.34	44.46	48.28	50.99
29	39.09	42.56	45.72	49.59	52.34
30	40.26	43.77	46.98	50.89	53.67
40	51.81	55.76	59.34	63.69	66.77
50	63.17	67.51	71.42	76.15	79.49