



CC32201 Applied Statistics I (Compulsory)

Paper info.	Theory (Part I) Total number of Questions: 4 Number of Pages: 5	INSTRUCTIONS Answer all four (04) questions. Only non-programmable calculators are permitted. Mobile phones are NOT permitted. Some useful test statistics and table critical values are given in Appendix 1.
Duration	2 (two) Hours	
Index No.		
		Date: June 30, 2026

1)

- a) State two commonly used measures of variability in a dataset. (2 marks)
- b) State the scale of measurement for each of the following variables. (5 marks)
- Average tomato yield (Mt/ha) in Kandy Districts *Sample*
 - COVID-19 vaccination status of a randomly selected person in Matara Town *Ratio*
 - A student's university registration number *Ordinal*
 - Order of finishing in a horse race *Nominal*
 - Average daytime temperature ($^{\circ}\text{C}$) in Mapalana *Interval*
- c) State three characteristics of the standard normal distribution. (3 marks)
- d) Sampling of an egg farm producing 500,000 eggs per week shows that the mean weight of individual eggs is 65 g with a standard deviation of 9 g. Assume that egg weights are normally distributed, calculate
- The number of eggs expected to weigh less than 55 g. (5 marks)
 - The number of eggs expected to weigh more than 70 g. (5 marks)
 - The number of eggs expected to weigh between 52 g and 56 g. (5 marks)

2)

- a)
- State the Central Limit Theorem. (3 marks)
 - State one situation in which Student's *t*-test is more appropriate than the *z*-test for testing a hypothesis about a population mean. (2 marks)
 - State three assumptions of Student's one-sample *t*-test. (6 marks)
- b) A researcher wishes to investigate the claim that the mean paddy yield in a certain area is 5.1 Mt/ha. Yield values were collected from 20 randomly selected 1-ha paddy fields. The sample mean and standard deviation were found to be 5.9 Mt/ha and 1.25 Mt/ha, respectively.

Assume that paddy yield is normally distributed.

- State the null and alternative hypotheses required to test the claim. (4 marks)
- Using a 5% significance level, test the hypothesis and state your conclusion. (6 marks)

- iii. Construct a 95% confidence interval for the true population mean yield.

(4 marks)

3)

A maize breeder at the National Crop Improvement Centre, Heavenland, has developed a new maize variety named **NutriMaize** and claims that it has a higher grain protein content (mg/g) than the existing variety **Golden Harvest**. To test this claim, 10 plots of each variety were cultivated under similar agronomic conditions. The protein contents (mg/g) measured from harvested grain samples are shown in Table 1. Assume that grain protein content is normally distributed.

Table 1. Grain protein content (mg/g) of two maize varieties

NutriMaize (X_1)	12.0	10.2	14.3	11.8	11.2	12.6	10.9	10.7	12.2	13.0	$\sum X_1$ = 118.9	$\sum X_1^2$ = 1427.1
Golden Harvest (X_2)	9.6	12.3	8.2	9.0	7.4	10.3	8.6	7.8	9.9	11.2	$\sum X_2$ = 94.3	$\sum X_2^2$ = 910.8

- a) State the null and alternative hypotheses. (4 marks)
- b) Using an appropriate statistical test, determine whether there is sufficient evidence to support the breeder's claim at the 5% significance level. Clearly show all calculations and interpret your findings. (16 marks)
- c) State three assumptions of the statistical test used in part ii). (5 marks)

4)

A researcher conducts a study to determine whether biting behaviour differs among puppies of different dog breeds. Random samples of puppies from three dog breeds were selected from various pet shops. Each puppy was observed over a two-week period and classified into one of the following categories: Not a biter, mild biter or flagrant biter. The results are summarised in Table 2.

Table 2. Observed frequencies of biting behaviour by dog breed

Breed	Not a biter	Mild biter	Flagrant biter	Row Total
Rottweiler	20	16	24	60
Boxer	30	10	10	50
Dalmatian	50	30	10	90
Column Total	100	56	44	200 (total observations)

- a) State two major applications of the *Chi-square test*. (4 marks)

- b) State the null and alternative hypotheses for testing the relationship between dog breed and biting behaviour. (4 marks)
- c) Using an appropriate *Chi-square test* at the 5% significance level, determine whether there is an association between dog breed and biting behaviour. Clearly show all calculations and interpret your findings. (15 marks)
- d) State two limitations of the *Chi-square test*. (2 marks)
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Appendix I – Useful test statistics and statistical tables

1. Student's *t*-statistic for two independent samples.

$$t = \frac{\bar{X}_1 - \bar{X}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

Where, $\bar{X}_1$ and $\bar{X}_2$ are sample means, s_1 and s_2 are the standard deviations of sample 1 and sample 2 respectively, and n_1 and n_2 are sample sizes. And the s is given by

$$s = \sqrt{\frac{\sum X^2 - \frac{(\sum X)^2}{n}}{n - 1}}$$

2. General equation for computing a confidence interval using the standard normal distribution:

$$CI_{1-\alpha} = \bar{X} \pm Z_{1-\alpha} \left(\frac{\sigma}{\sqrt{n}} \right)$$

$Z_{1-\alpha}$ is the table critical Z value from the standard normal distribution at a given significance level

3. General equation for computing a confidence interval using the Student's *t* distribution:

$$CI_{1-\alpha} = \bar{X} \pm t_{1-\alpha} \left(\frac{s}{\sqrt{n}} \right)$$

Where, $\bar{X}$ is the sample mean, s is the sample standard deviation and n is the sample size and $t_{1-\alpha}$ is the table critical value at a given significance level α , and at a given degrees of freedom

1.219

Statistical tables

1. Student's t distribution – Critical values of t (only a part of the table is displayed)

t Table

cum. prob	$t_{.50}$	$t_{.75}$	$t_{.80}$	$t_{.85}$	$t_{.90}$	$t_{.95}$	$t_{.975}$	$t_{.99}$	$t_{.995}$	$t_{.999}$	$t_{.9995}$
one-tail	0.50	0.25	0.20	0.15	0.10	0.05	0.025	0.01	0.005	0.001	0.0005
two-tails	1.00	0.50	0.40	0.30	0.20	0.10	0.05	0.02	0.01	0.002	0.001
df											
1	0.000	1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.31	636.62
2	0.000	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	22.327	31.599
3	0.000	0.765	0.978	1.250	1.638	2.353	3.182	4.541	5.841	10.215	12.924
4	0.000	0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	0.000	0.727	0.920	1.156	1.476	2.015	2.571	3.365	4.032	5.893	6.869
6	0.000	0.718	0.906	1.134	1.440	1.943	2.447	3.143	3.707	5.208	5.959
7	0.000	0.711	0.896	1.119	1.415	1.895	2.365	2.998	3.499	4.785	5.408
8	0.000	0.706	0.889	1.108	1.397	1.860	2.306	2.896	3.355	4.501	5.041
9	0.000	0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.297	4.761
10	0.000	0.700	0.879	1.093	1.372	1.812	2.228	2.764	3.169	4.144	4.587
11	0.000	0.697	0.876	1.088	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	0.000	0.695	0.873	1.083	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	0.000	0.694	0.870	1.079	1.350	1.771	2.160	2.650	3.012	3.852	4.221
14	0.000	0.692	0.868	1.076	1.345	1.761	2.145	2.624	2.977	3.787	4.140
15	0.000	0.691	0.866	1.074	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16	0.000	0.690	0.865	1.071	1.337	1.746	2.120	2.583	2.921	3.686	4.015
17	0.000	0.689	0.863	1.069	1.333	1.740	2.110	2.567	2.898	3.646	3.965
18	0.000	0.688	0.862	1.067	1.330	1.734	2.101	2.552	2.878	3.610	3.922
19	0.000	0.688	0.861	1.066	1.328	1.729	2.093	2.539	2.861	3.579	3.883
20	0.000	0.687	0.860	1.064	1.325	1.725	2.086	2.528	2.845	3.552	3.850

2. Standard normal distribution table

STANDARD NORMAL DISTRIBUTION: Table Values Represent AREA to the LEFT of the Z score.

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.9	.00005	.00005	.00004	.00004	.00004	.00004	.00004	.00004	.00003	.00003
-3.8	.00007	.00007	.00007	.00006	.00006	.00006	.00006	.00005	.00005	.00005
-3.7	.00011	.00010	.00010	.00010	.00009	.00009	.00008	.00008	.00008	.00008
-3.6	.00016	.00015	.00015	.00014	.00014	.00013	.00013	.00012	.00011	.00011
-3.5	.00023	.00022	.00022	.00021	.00020	.00019	.00019	.00018	.00017	.00017
-3.4	.00034	.00032	.00031	.00030	.00029	.00028	.00027	.00026	.00025	.00024
-3.3	.00048	.00047	.00045	.00043	.00042	.00040	.00039	.00038	.00036	.00035
-3.2	.00069	.00066	.00064	.00062	.00060	.00058	.00056	.00054	.00052	.00050
-3.1	.00097	.00094	.00090	.00087	.00084	.00082	.00079	.00076	.00074	.00071
-3.0	.00135	.00131	.00126	.00122	.00118	.00114	.00111	.00107	.00104	.00100
-2.9	.00187	.00181	.00175	.00169	.00164	.00159	.00154	.00149	.00144	.00139
-2.8	.00256	.00248	.00240	.00233	.00226	.00219	.00212	.00205	.00199	.00193
-2.7	.00347	.00336	.00326	.00317	.00307	.00298	.00289	.00280	.00272	.00264
-2.6	.00466	.00453	.00440	.00427	.00415	.00402	.00391	.00379	.00368	.00357
-2.5	.00621	.00604	.00587	.00570	.00554	.00539	.00523	.00508	.00494	.00480
-2.4	.00820	.00798	.00776	.00755	.00734	.00714	.00695	.00676	.00657	.00639
-2.3	.01072	.01044	.01017	.00990	.00964	.00939	.00914	.00889	.00866	.00842
-2.2	.01390	.01355	.01321	.01287	.01255	.01222	.01191	.01160	.01130	.01101
-2.1	.01786	.01743	.01700	.01659	.01618	.01578	.01539	.01500	.01463	.01426
-2.0	.02275	.02222	.02169	.02118	.02068	.02018	.01970	.01923	.01876	.01831
-1.9	.02872	.02807	.02743	.02680	.02619	.02559	.02500	.02442	.02385	.02330
-1.8	.03593	.03515	.03438	.03362	.03288	.03216	.03144	.03074	.03005	.02938
-1.7	.04457	.04368	.04272	.04182	.04093	.04006	.03920	.03836	.03754	.03673
-1.6	.05480	.05379	.05262	.05155	.05050	.04947	.04846	.04746	.04648	.04551
-1.5	.06681	.06552	.06426	.06301	.06178	.06057	.05938	.05821	.05705	.05592
-1.4	.08076	.07927	.07780	.07636	.07493	.07353	.07215	.07078	.06944	.06811
-1.3	.09680	.09510	.09342	.09176	.09012	.08851	.08691	.08534	.08379	.08226
-1.2	.11507	.11314	.11123	.10935	.10749	.10565	.10383	.10204	.10027	.09853
-1.1	.13567	.13350	.13136	.12924	.12714	.12507	.12302	.12100	.11900	.11702
-1.0	.15866	.15625	.15386	.15151	.14917	.14686	.14457	.14231	.14007	.13786
-0.9	.18406	.18141	.17879	.17619	.17361	.17106	.16853	.16602	.16354	.16109
-0.8	.21186	.20897	.20611	.20327	.20045	.19766	.19489	.19215	.18943	.18673
-0.7	.24196	.23885	.23576	.23270	.22965	.22663	.22363	.22065	.21770	.21476
-0.6	.27425	.27093	.26763	.26435	.26109	.25785	.25463	.25143	.24825	.24510
-0.5	.30854	.30503	.30153	.29806	.29460	.29116	.28774	.28434	.28096	.27760
-0.4	.34458	.34090	.33724	.33360	.32997	.32636	.32276	.31918	.31561	.31207
-0.3	.38209	.37828	.37448	.37070	.36693	.36317	.35942	.35569	.35197	.34827
-0.2	.42074	.41683	.41294	.40905	.40517	.40129	.39743	.39358	.38974	.38591
-0.1	.46017	.45620	.45224	.44828	.44433	.44038	.43644	.43251	.42858	.42465
-0.0	.50000	.49601	.49202	.48803	.48405	.48006	.47608	.47210	.46812	.46414

STANDARD NORMAL DISTRIBUTION: Table Values Represent AREA to the LEFT of the Z score.

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.50000	.50399	.50798	.51197	.51595	.51994	.52392	.52790	.53188	.53586
0.1	.53983	.54380	.54776	.55172	.55567	.55962	.56356	.56749	.57142	.57535
0.2	.57926	.58317	.58706	.59095	.59483	.59871	.60257	.60642	.61026	.61409
0.3	.61791	.62172	.62552	.62930	.63307	.63683	.64058	.64431	.64803	.65173
0.4	.65542	.65910	.66276	.66640	.67003	.67364	.67724	.68082	.68439	.68793
0.5	.69146	.69497	.69847	.70194	.70540	.70884	.71226	.71566	.71904	.72240
0.6	.72575	.72907	.73237	.73565	.73891	.74215	.74537	.74857	.75175	.75490
0.7	.75804	.76115	.76424	.76730	.77035	.77337	.77637	.77935	.78232	.78524
0.8	.78814	.79103	.79489	.79873	.79955	.80234	.80511	.80785	.81057	.81327
0.9	.81594	.81859	.82121	.82381	.82639	.82894	.83147	.83398	.83646	.83891
1.0	.84134	.84375	.84614	.84849	.85083	.85314	.85543	.85769	.85993	.86214
1.1	.86433	.86650	.86864	.87076	.87286	.87493	.87698	.87900	.88100	.88298
1.2	.88493	.88689	.88877	.89065	.89251	.89435	.89617	.89796	.89973	.90147
1.3	.90320	.90490	.90658	.90824	.90988	.91149	.91309	.91466	.91621	.91774
1.4	.91924	.92073	.92220	.92364	.92507	.92647	.92785	.92922	.93056	.93189
1.5	.93319	.93448	.93574	.93699	.93822	.93943	.94062	.94179	.94295	.94408
1.6	.94520	.94630	.94738	.94845	.94950	.95053	.95154	.95254	.95352	.95449
1.7	.95543	.95637	.95728	.95818	.95907	.95994	.96080	.96164	.96246	.96327
1.8	.96407	.96485	.96562	.96638	.96712	.96784	.96856	.96926	.96995	.97062
1.9	.97128	.97193	.97257	.97320	.97381	.97441	.97500	.97558	.97615	.97670
2.0	.97725	.97778	.97831	.97882	.97932	.97982	.98030	.98077	.98124	.98169
2.1	.98214	.98257	.98300	.98341	.98382	.98422	.98461	.98500	.98537	.98574
2.2	.98610	.98645	.98679	.98713	.98745	.98778	.98809	.98840	.98870	.98899
2.3	.98928	.98956	.98983	.99010	.99036	.99061	.99086	.99111	.99134	.99158
2.4	.99180	.99207	.99234	.99259	.99286	.99310	.99334	.99357	.99380	.99402
2.5	.99425	.99448	.99471	.99494	.99516	.99538	.99560	.99581	.99602	.99623
2.6	.99644	.99665	.99686	.99706	.99726	.99745	.99764	.99782	.99799	.99816
2.7	.99833	.99850	.99867	.99883	.99898	.99913	.99927	.99940	.99953	.99966
2.8	.99979	.99991	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
2.9	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.0	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.1	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.2	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.3	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.4	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.5	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.6	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.7	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.8	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999
3.9	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999	.99999

3. Chi-Square distribution table (only a part of the table is displayed)

Chi-square Distribution Table

d.f.	.995	.99	.975	.95	.9	.1	.05	.025	.01
1	0.00	0.00	0.00	0.00	0.02	2.71	3.84	5.02	6.63
2	0.01	0.02	0.05	0.10	0.21	4.61	5.99	7.38	9.21
3	0.07	0.11	0.22	0.35	0.58	6.25	7.81	9.35	11.34
4	0.21	0.30	0.48	0.71	1.06	7.78	9.49	11.14	13.28
5	0.41	0.55	0.83	1.15	1.61	9.24	11.07	12.83	15.09
6	0.68	0.87	1.24	1.64	2.20	10.64	12.59	14.45	16.81
7	0.99	1.24	1.69	2.17	2.83	12.02	14.07	16.01	18.48
8	1.34	1.65	2.18	2.73	3.49	13.36	15.51	17.53	20.09
9	1.73	2.09	2.70	3.33	4.17	14.68	16.92	19.02	21.67
10	2.16	2.56	3.25	3.94	4.87	15.99	18.31	20.48	23.21